

# Feature Extraction From Large-scale Data in Power Grid to Identify and Locate Events in Real-time

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# Outline

- 1 Background
- 2 Low-dimensionality Structure of PMU Data & Fast Event Identification
- 3 Real-time Fault Location through Deep Learning
- 4 Conclusions and Future Work

# Background

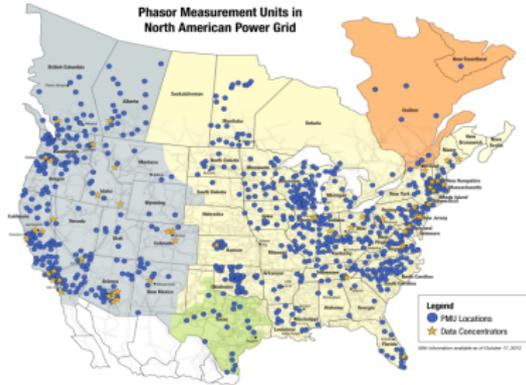


Figure: Installation of PMUs in the North America <https://www.naspi.org/documents>

- **Phase measurement units (PMU)** provide synchronized phasor measurements at the sampling rate of 30 or 60 sample per second;
- More than **2000** PMU are installed in the North America.
- PMU are generating large-scale of datasets in the power grid;
- **Data-driven** methods based on PMU data are promising to **automatically locate and identify** abnormal conditions in power grid.

## Challenges and Opportunities

- For the **large-scale high dimensional** PMU data, how to extract useful information ?
- How to **connect the variations of data with the physical modeling** to monitor, adjust and optimize the current modeling ?
- How to propose **efficient and accurate algorithms** based on the PMU data to participate the closed-loop control?
- How to **reveal the correlations** in the data to augment our understanding of the system states?

## Low-dimensional Structure of PMU data

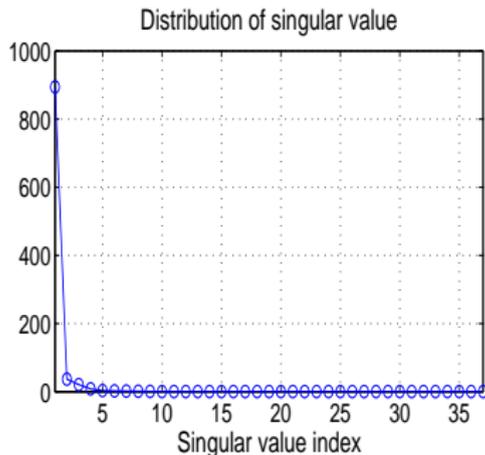
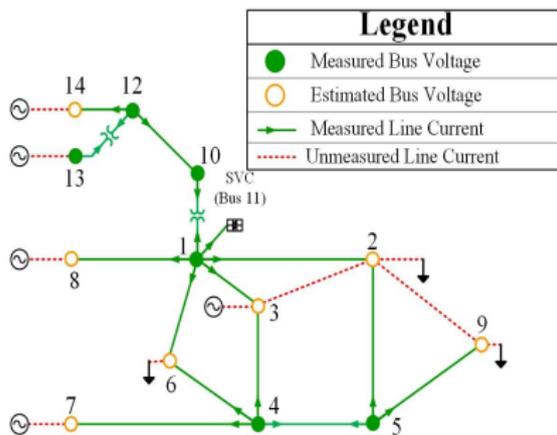


Figure: PMUs in Central NY Power Systems

Figure: Singular values of the PMU data matrix

- 37 voltage/current phasors. 30 samples/second for 20 seconds. Form a large matrix of 600 by 37.
- Singular values decay significantly. Mostly close to zero. Singular values can be approximated by a sparse vector.
- Low-dimensionality also used in [Chen, Xie, Kumar 2013, Dahal, King, Madani 2012] for dimensionality reduction.

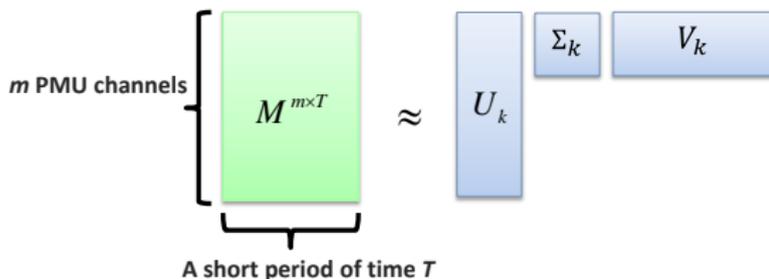
## Motivations of Identifying Events

- Fast event identification is important to prevent cascading failures and enhance system security ;
- The existing data-driven methods have some limitations:
  - large dictionary size & complicated training: 6000 root patterns in a 21-bus system [Wang W et al., 2014], several hidden Markov models are trained to detect and identify events [Jiang H et al., 2014].
  - off-line algorithms & long window size: [Song Y et al., 2015] employed an off-line algorithm of 20-second data ;
  - high sampling frequency: [Jiang H et al., 2014] utilized 1kHz sampling rate based on frequency disturbance recorder;

## Problem Formulation and Feature Extraction

- **Problem:** Given the PMU data  $M \in R^{m \times T}$  of  $m$  buses in the time period  $T$ , we want to identify events like line trip, generator trip, line fault.
- **Main Idea:** Extract features and establish a dictionary;
- Extract **feature matrix**  $V_k \in R^{T \times k}$ ,  $k \ll m$ ,  $k \ll T$  by singular value decomposition (SVD) in (1);

$$M = U_k \Sigma_k V_k \quad (1)$$



$U_k, V_k$  : span column and row subspaces;  
 $\Sigma_k$  : the  $k$  largest singular values of  $M$ .

## Physical interpretation of feature matrix $V_k$

- A linear model after an impulse input follows

$$\begin{aligned}x(t+1) &= Ax(t) + Bu(t) \\ y(t) &= Cx(t)\end{aligned}$$

where  $x(t), y(t)$  are the deviation of state variable and measurements at time  $t$ ,  $u(t)$  is the input variable, and  $A, B, C$  are the state matrix, input matrix and observation matrix

- Let  $\beta_k^\dagger = [\lambda_k, \lambda_k^2, \dots, \lambda_k^T]$ , where  $\lambda_k$  are the  $k$ th eigenvalue of  $A$ ;
- $\text{Span}(V_k) = \text{Span}(\beta)$  assume that in a short time  $u(t) \sim 0$
- Various types of events excite distinctive eigenvalues thus  $V_k$  are different;
- $V_k$  can represent different dynamics after events.

## Our Approach: Event Identification through Dictionary

- Identify an event by comparing the row subspace of the real-time spatial-temporal PMU data blocks with a dictionary of subspaces obtained from recorded PMU data with known event types.

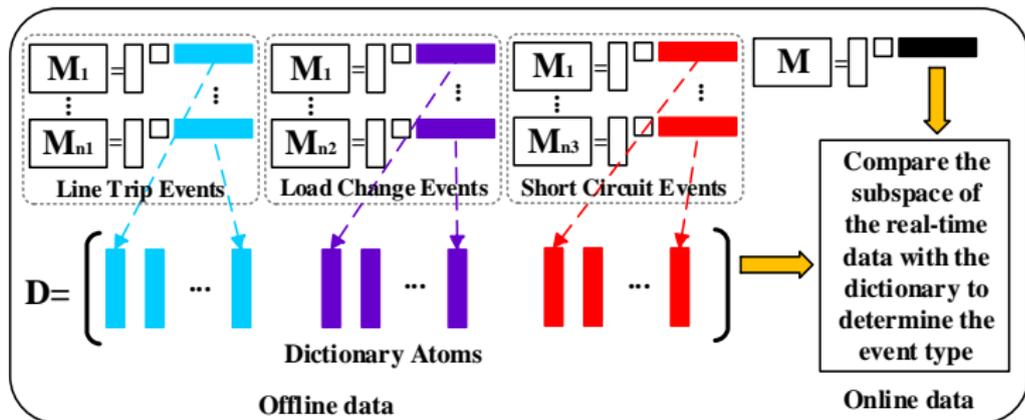


Figure: Dictionary construction from historical datasets and real-time data identification through subspace comparison

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## Similarity of Subspaces

- Subspace Angle [Mahdi S et al., 2014]

$$\theta(\mathcal{S}_l, \mathcal{S}_k) = \arccos(\sqrt{\|B_k^\dagger B_l\|_F^2 / \min\{k, l\}}). \quad (2)$$

- $\theta$  equals  $90^\circ$  if two subspaces are orthogonal to each other;
- $\theta$  equals  $0^\circ$  if two subspaces are the same ( $l = k$ ) or one is embedded in the other ( $l \neq k$ ).
- A smaller  $\theta$  indicates higher affinity of two subspaces.

## Experimental Results of ISO NE PMU data

Table: Minimum subspace angles between a test case and the dictionary atoms of three types of events in recorded PMU data

Events \ Dictionary	Load Change	Fault	Line Trip
Load Change 1	<b>4.08°</b>	16.91°	18.29°
Load Change 2	<b>3.12°</b>	20.81°	14.39°
Fault 1	24.95°	<b>6.33°</b>	23.86°
Fault 2	8.93°	<b>3.73°</b>	15.76°
Line Trip 1	7.25°	5.85°	<b>3.93°</b>
Line Trip 2	11.20°	30.21°	<b>4.27°</b>

- The minimum subspace angle (bolded) indicates the type of the events;
- 32 events of three types are tested with 100 % identification accuracy rate.

## Motivations of Locating Faults

- Locating faults in real time is crucial to improve the power system **stability and reliability**;
- Impedance-based methods often **assume loads are static** and are sensitive to topology change;
- Traveling-wave-based method require **high sampling rate and accuracy** of measurements;
- Artificial intelligent methods: some require high sampling rate like 2400 Hz (Mehrdad 17), some are DC model based, some only **for single type** of faults or single transmission line and **complete observability of the system** required ( Guangyu 16).

## Problem Formulation

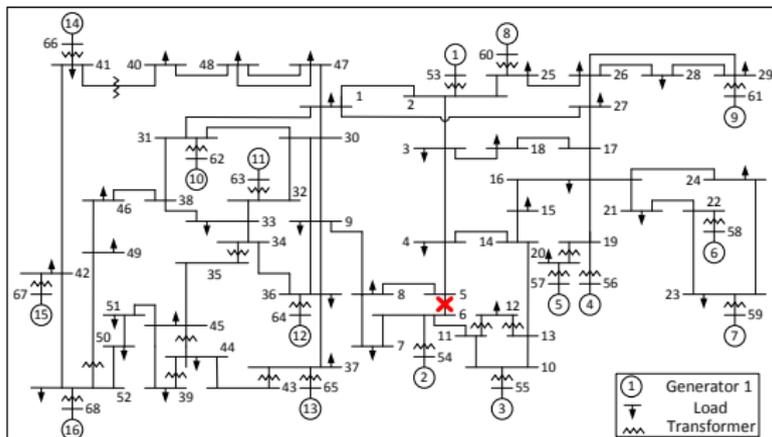


Figure: The line 5-6 is faulted in the IEEE 68-bus power system

- **Problem:** When a line is faulted (marked as red cross), how to locate the fault efficiently?
- **Challenges:**
  - The **type** of fault can be various, including symmetrical or asymmetrical fault;
  - Various **fault impedances** cause voltage drop in different degree;
- **Our Approach:**
  - Extract location features;
  - Classify by a convolutional neural network (CNN).

## Feature Extraction

Given voltage PMU data of the power system with  $n$  buses before and during fault  $U^0, U' \in \mathcal{C}^n$  and admittance matrix  $Y^0 \in \mathcal{C}^{n \times n}$  before the fault and  $\Delta U = U^0 - U'$ , we define the **feature vector**  $\psi \in \mathcal{C}^n$  in (3):

$$\psi = Y^0 \Delta U \quad (3)$$

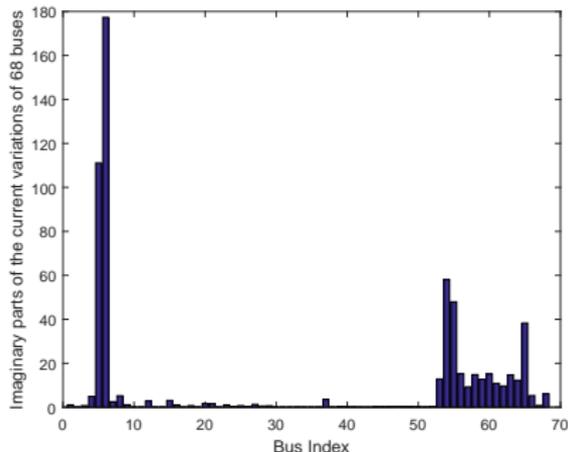


Figure: The imaginary parts of the feature vector  $\psi$  after the line 5-6 is faulted

- **Physical Interpretation of  $\psi$ :**  
Based on the **substitution theory**,

$$\psi = \Delta I^u + \Delta I \quad (4)$$

where  $\Delta I^u$  is a sparse vector with nonzero values only at the terminal buses of the faulted line;  $\Delta I$  denotes the current variations of buses.

## Our CNN Classifier

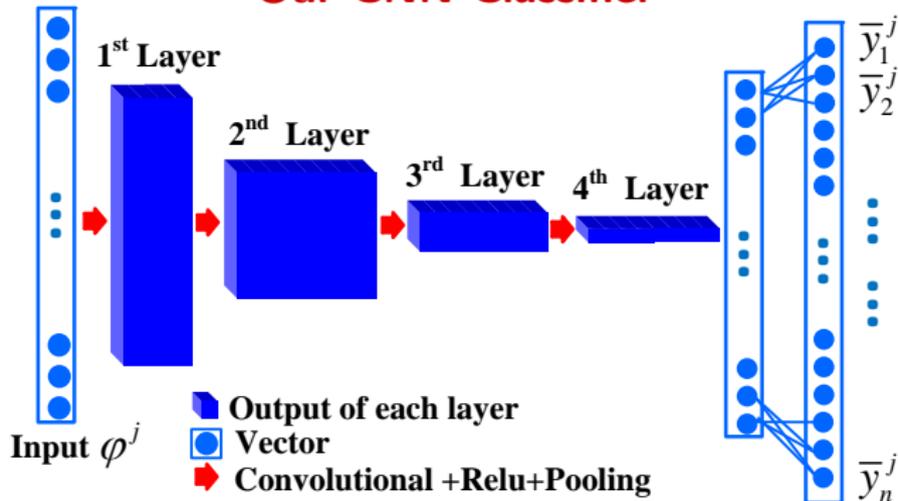


Figure: Understanding CNN

- Input the extracted feature  $\psi^j$  and the label  $y^j$  of the  $j$ th dataset;
- CNN optimizes the parameters by minimizing a loss function, and then outputs  $\bar{y}_i^j$ , **the probability of the  $i$ th line** for the  $j$ th dataset;
- The line with the highest probability indicates the faulted line.

## Numerical Results

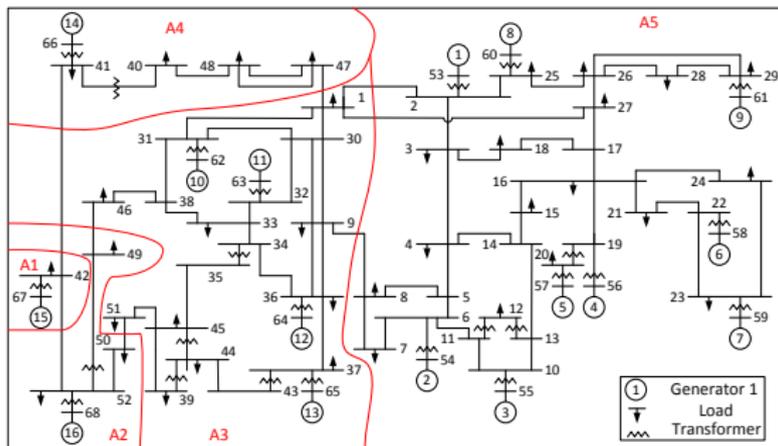


Figure: The IEEE 68-bus Power System

- Four types of faults, including three phase (**TP**), line to ground (**LG**), double line to ground (**DLG**) and line to line (**LL**) faults, are simulated in the IEEE 68-bus power system;
- More than 2300 datasets of **various locations, different types and fault impedances, and random load fluctuations** are generated;
- Data rate is 30 samples per second.

## Location Accuracy with Complete Measurements

Table: The LAR  $\eta$  (%) of **MSVM**

$Z_f$ (p.u.)	0.05	0.01	0.001	0.0001
LAR of TP (%)	100	100	100	100
LAR of LG (%)	100	100	100	100
LAR of DLG (%)	98.6	100	100	99.5
LAR of LL (%)	98.6	99.6	93.5	94.6

Table: The LAR  $\eta$  (%) of **CNN** or **NN**

$Z_f$ (p.u.)	0.05	0.01	0.001	0.0001
LAR of TP (%)	100	100	100	100
LAR of LG (%)	100	100	100	100
LAR of DLG (%)	100	100	100	100
LAR of LL (%)	100	100	100	100

- The location accuracy rate (**LAR**)<sup>1</sup> of Multi-class support vector machine (**MSVM**), Neural Network(**NN**) and **CNN** are all more than 90% for most events when the system is **completely measured**.

<sup>1</sup>defined as  $\eta = \frac{\text{The number of faults correctly located}}{\text{total number of faults}}$

## Location Accuracy with Partial Measurements

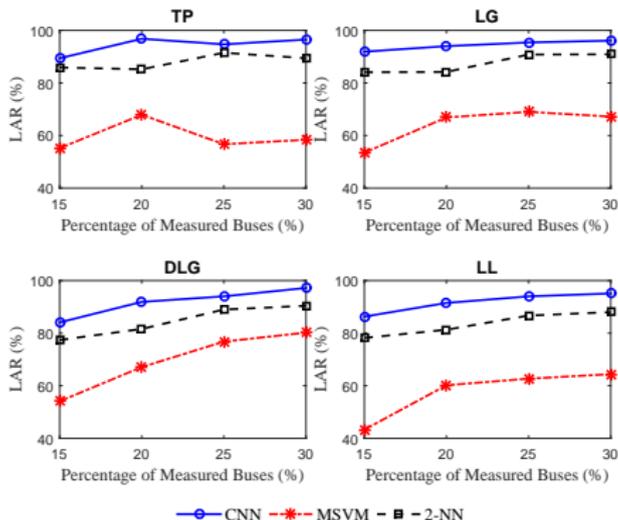


Figure: The LAR of the CNN, MSVM, NN with different percentage of measured buses

- When **15 % ~ 30 %** buses are measured, the LAR of CNN is **higher** than that of MSVM and NN for different types of faults;
- When at least **30 %** buses are measured, the location accuracy of CNN can be higher than 95%;
- What if less than **15 %** ?

## Performance When $\leq 15\%$ Buses are Measured

Table: The ARC of CNN on different types of events with the ratio of measured buses less than 15%

Measured Ratio	TP	LG	DLG	LL
7 %	1.32	1.48	1.92	1.56
10 %	1.38	1.28	1.66	1.54
15 %	1.38	1.23	1.57	1.54

- Define Averaged Rank of the Correct (**ARC**) line to indicate how many lines that mostly include the correct lines;
- **The ARC, less than 3**, when  $\leq 15\%$  ratios of buses are measured, indicates that most correct lines are in the lines having the **top-3 probability**;
- **Moreover**, the lines with high probability are mostly near the faulted line.

## Example: Line 5-6 is faulted

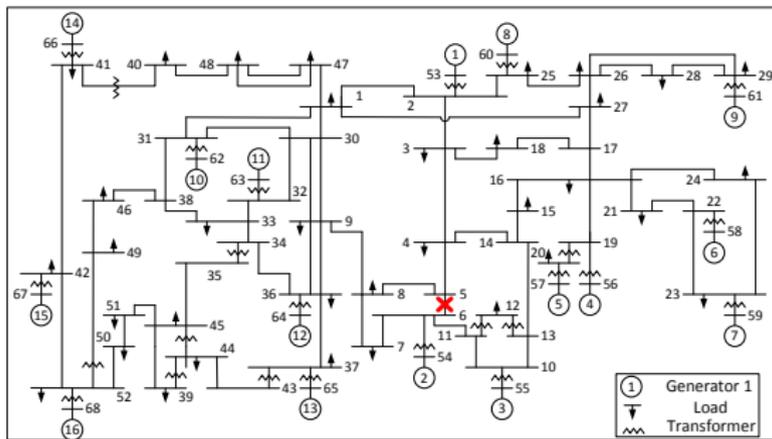


Figure: The lines with the top-5 probability when only 5 buses are measured

- Only **7%** buses are measured;
- The correct line 5-6 has the **second highest probability**;

## The Lines with Top-5 Probability

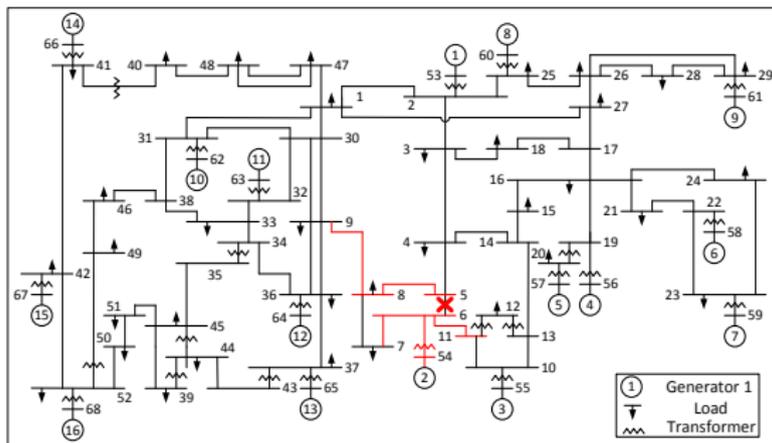


Figure: The lines with the top-5 probability when only 5 buses are measured

- The lines with the top-5 probability marked in red are **in the neighborhood** of the faulted line 5-6;
- This neighborhood property is **not a special case** but commonly exist in most cases;
- **Why** the lines with high probability show the neighborhood property? is it coincidence or due to some magic of CNN?

## The essence of the neighborhood property

- It is verified that the neighborhood property exist even **other classifier like NN** is applied;

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- For the  $k$ th (  $k \neq i, j$  ) entry  $\psi_k$  when the line  $i$ - $j$  is faulted:

$$\psi_k = \Delta I_k + \Delta I_k^u = \Delta I_k \quad (6)$$

$$= \sum_{j \in \mathcal{N}_k} Y_{kj}^0 \Delta U_j \quad (7)$$

where  $Y_{kj}^0$  denotes the admittance between bus  $k$  and  $j$  before the fault, and  $\mathcal{N}_k$  denotes **the neighbor of the bus  $k$** .

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- Thus  $\psi_k$  denotes the sum of the total current variations in the neighborhood of  $k$ .

## Greedy Algorithm of PMU Placement

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**Algorithm 1** Greedy Algorithm to Select PMU Placement

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- 1: Input parameters:  $m, \beta = 1$
  - 2: Initialize :  $\mathcal{S}_0 = \emptyset$  and the loss value  $l = \infty$
  - 3: **for**  $k = 0, \dots, m$  **do**
  - 4:   **for** bus  $i = 1, \dots, n$  **do**
  - 5:     Compute the minimum loss  $l_i = \min_{\Theta} l(\Theta, \{\mathcal{S}_k \cup i\})$   
of (1) for each bus  $i$
  - 6:   **end for**
  - 7:    $i^* = \arg \min_i (\frac{\beta}{d_i} + l_i)$ ,
  - 8:   where  $d_i$  the degree of bus  $i$ ,  $\beta$  is a weight parameter.
  - 9:   **if**  $l_{i^*} < l$  **then**
  - 10:      $\mathcal{S}_{k+1} = \mathcal{S}_k \cup i^*$
  - 11:      $l = l_{i^*}$
  - 12:   **else**
  - 13:      $\mathcal{S}_{k+1} = \mathcal{S}_k$
  - 14:   **end if**
  - 15: **end for**
  - 16: Output:  $\mathcal{S}_m$
- 

The loss function is (1) is:

$$l'(\Theta, \mathcal{S}) = \min_{\Theta} \frac{1}{N} \sum_{j=1}^N \sum_{i=1}^n y_i^j \log \bar{y}_i^j(\Theta, \mathcal{S}) + \lambda \|\Theta\|_F^2$$

## Performances Comparison of Different Algorithms

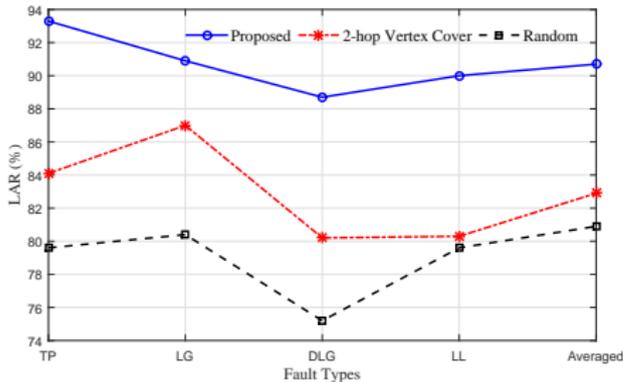


Figure: LAR of CNN based on different algorithms

- The LAR of the four types of faults are compared when about 15% buses are measured by different algorithms;
- The “2-hop Vertex Cover” method is only based on the graph connectivity and “Random” method is to select buses arbitrarily;
- The proposed algorithm achieves a better location accuracy rate for different types of faults.

## Conclusions & Future Work

- **A real time** fault location method is proposed based on a CNN classifier;
- This method can keep a high location accuracy when the system is **fully or partially** measured;
- Our CNN classifier achieves a higher LAR than that of the MSVM and NN when the system is partially measured;
- **The lines with high probabilities** can indicate the small area of the faulted line;
- The proposed PMU placement algorithm can improve the location accuracy rate;
- More sensitivity of our method will be tested in the **future work**.

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